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**ADDENDUM**  
**TO**  
**IDENTIFYING AND ANALYZING METHODS FOR REDUCING**  
**THE ENERGY CONSUMPTION OF HELICOPTERS**

By

S. Jon Davis  
Harold J. Rosenstein

Prepared under Contract No. NAS1-13624

By

Boeing Vertol Company  
Philadelphia, Pennsylvania

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**NATIONAL AERONAUTICS AND SPACE ADMINISTRATION**

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## LIST OF SYMBOLS AND ABBREVIATIONS

|                             |  |
|-----------------------------|--|
| Btu                         | British thermal unit   |
| b                           | rotor-blade number   |
| c                           | rotor-blade chord, ft  |
| $C_p$                       | rotor power coefficient, $550 \text{ hp}/\rho\pi R^2 V_{\text{TIP}}^3$ |
| $C_T$                       | rotor thrust coefficient, $T/\rho\pi R^2 V_{\text{TIP}}^2$             |
| DOC                         | direct operating cost, \$/seat-mile                                    |
| EI                          | energy intensity, Btu/passenger-n mi                                   |
| $EW_{\text{STR}}/\text{GW}$ | structural empty-to-gross weight ratio                                 |
| $F_e$                       | equivalent flat-plate drag area, $\text{ft}^2$                         |
| FM                          | helicopter rotor figure of merit, $0.707 C_T^{3/2}/C_p$                |
| HOEI                        | hover, one engine inoperative  |
| HP                          | power, horsepower  |
| KTAS                        | knots true airspeed  |
| $L/D_e$                     | rotor lift-to-effective drag ratio                                     |
| N MI                        | nautical miles   |
| NRP                         | normal rated or maximum continuous power                               |
| R                           | rotor radius, ft   |
| SFC                         | specific fuel consumption, lb fuel/hr/hp                               |
| T                           | thrust, lb   |
| T/W                         | rotor thrust-to-gross weight ratio                                     |
| $V_{\text{BR}}$             | best-range cruising speed  |
| $V_{\text{NRP}}$            | normal-rated-power cruising speed                                      |
| $V_{\text{TIP}}$            | rotor tip speed, ft/sec  |
| W/A                         | helicopter rotor disk loading, $\text{lb}/\text{ft}^2$                 |
| $\rho$                      | atmospheric density, slugs/ $\text{ft}^3$                              |
| $\sigma$                    | rotor solidity, $\frac{bc}{\pi R}$                                     |

## 1.0 INTRODUCTION

Previous studies have shown that, on the basis of fuel efficiency, current production helicopters can be competitive with other forms of transportation. Reductions in helicopter energy consumption can be accomplished through the use of advanced technology in the areas of powerplant design, improved rotor efficiency, reduced parasite drag, and reduced structural empty weight.

In the main body of this report, baseline helicopters incorporating today's technology were designed for a short range (200 n mi) and a very short-haul (100 n mi) mission scenario. Parametric analyses were then conducted to determine the impact of technology improvement.

Many of the parameters varied are interrelated. This addendum presents a summary of such interactions and adds some additional sensitivity values so that energy reduction and DOC as affected by the major technological factors or operational modes are clearly defined. Table 1 presents a summary of the technological improvements (and their associated EI reductions) to be addressed in the following paragraphs.

TABLE 1. SUMMARY OF PROJECTED TECHNOLOGICAL IMPROVEMENTS  
AND THEIR EFFECT ON ENERGY INTENSITY

| Technological Area                                | Percent Improvement | Percent Reduction in Energy Intensity |
|---|---------------------|---------------------------------------|
| Improved Engine SFC (conventional engines)        | 4.76% reduction     | 5.8%                                  |
| Improved Engine SFC (regenerative engines)        | 14.3% reduction     | 16.6%                                 |
| Reduced Parasite Drag                             | 54% reduction       | 3.1%                                  |
| Improved Cruise Efficiency (rotor $L/D_e$ )       | 20% increase        | 6.5%                                  |
| Improved Hover Efficiency (rotor figure of merit) | 9.3% increase       | 9.2%                                  |
| Reduced Structural Empty/Gross Weight             | 12.1% reduction     | 12.5%                                 |

## 2.0 MATCHED HELICOPTERS

In both CR-144953 and this addendum, reference is made to the matched helicopter. Such a matched helicopter is defined as a configuration having sufficient rotor solidity to allow its rotor limit and NRP cruising speeds to be equal. (It is worth noting that such matched vehicles exhibit minimum DOC values because of their ability to operate at NRP cruising speed.) Vehicles having less solidity are rotor-limited to a lower cruising speed.

The sizing of matched helicopters can introduce significant EI penalties. Accordingly, a more detailed discussion of the relative merits of matched versus unmatched helicopters is in order.

As an example, if the parasite-drag level of a given vehicle is reduced and the vehicle is resized with no accompanying change in solidity, the resulting helicopter will have the capability to fly at a higher cruising speed but will be limited to the rotor-limit cruising speed dictated by the solidity. Being limited to this cruising speed and operating at a reduced power required results in a reduced fuel-consumption rate. Therefore, this unmatched vehicle exhibits a significant reduction in EI compared to the original vehicle. However, since it is operating at a cruising speed less than its potential NRP cruising speed, it also exhibits an increased DOC (compared to the original vehicle).

If the original vehicle is again resized at a reduced parasite-drag level, and the rotor solidity is increased to allow operation at a higher cruising speed, several things occur:

1. The structural empty-weight fraction increases, reflecting the increased solidity.
2. The increased structural empty weight causes an escalation in the gross weight.
3. Since the helicopter is not rotor-limited and can fly faster, the fuel consumption is increased.

The resulting matched helicopter thus exhibits less of an EI reduction relative to the original vehicle than the corresponding unmatched helicopter.

In summary, then, helicopters which are rotor-limited (i.e., unmatched) exhibit greater reductions in EI than those which are matched in such a way as to allow rotor-limit and NRP speeds to coincide. However, helicopters which cruise at speeds lower than NRP speed have higher DOC's than matched vehicles.

Since minimum-DOC operation is an important criterion for commercial helicopters, the study of CR-144953 emphasized the sizing of matched, minimum-DOC helicopters. The fact remains, however, that any choice between matched and unmatched helicopters must reflect a conscious choice between energy reduction and minimum-DOC operation.



## 3.0 RESULTS AND DISCUSSION

### 3.1 Presentation of Results

The type of graphic presentation used in this addendum for illustrating the interactions of Energy Intensity (EI) and Direct Operating Cost (DOC) with cruising speed is a vector representation. This allows a more complete display of the factors involved in EI or DOC reduction than bar charts or tables alone.

Figure 1 is a diagrammatic representation of such a typical EI vector diagram. Note that the vector's origin (point A) always corresponds to the EI value for the current technology (1975), compromise design-point helicopter. Note also that the end point of the vector (points B, C, or D) corresponds to the EI value of a resized helicopter incorporating either changes in technology level or design ground rules. Thus, the resulting vector illustrates both the magnitude and direction of the EI and cruising-speed changes obtained for such modifications in technology level or design ground rules. For example, vector AB illustrates a reduction in EI accompanied by an increase in cruising speed; vector AC illustrates a reduction in EI at a constant cruising speed; and vector AD represents a decrease in cruising speed at a constant EI level. It should be further noted that these EI-cruising speed vectors can be added together vectorially. This is illustrated in Figure 2, where vectors representing various technological modifications are added together to create a resultant vector incorporating all the individual technological changes.

### 3.2 Results

**3.2.1 Effect of technological advances on matched aircraft.** – Figure 2 presents in graphic form the effects of the following on Btu/passenger mile and DOC for matched aircraft.

Each vector represents the change (from the baseline value) in EI and cruising speed due to a given technological improvement.

For clarity's sake, the vector for a 4.76-percent reduction in SFC has not been included. It has the same direction as the 14.3-percent SFC reduction vector, but a smaller magnitude.

Vector ① represents a 14.3-percent reduction in engine SFC due to incorporation of regenerative-engine technology. Reduction in SFC results (because of the iterative nature of the sizing process) in a reduction in vehicle gross weight. Note, however, that this does not result in any change in vehicle cruising/rotor-limit speed.

Vector ② represents a 54-percent reduction in vehicle parasite drag. Reduced parasite power required enables the helicopter to fly faster for the same amount of installed power. However, rotor solidity must be increased to allow the helicopter to fly faster without encountering the rotor limit. Thus, matching the helicopter NRP cruising and rotor-limit speeds

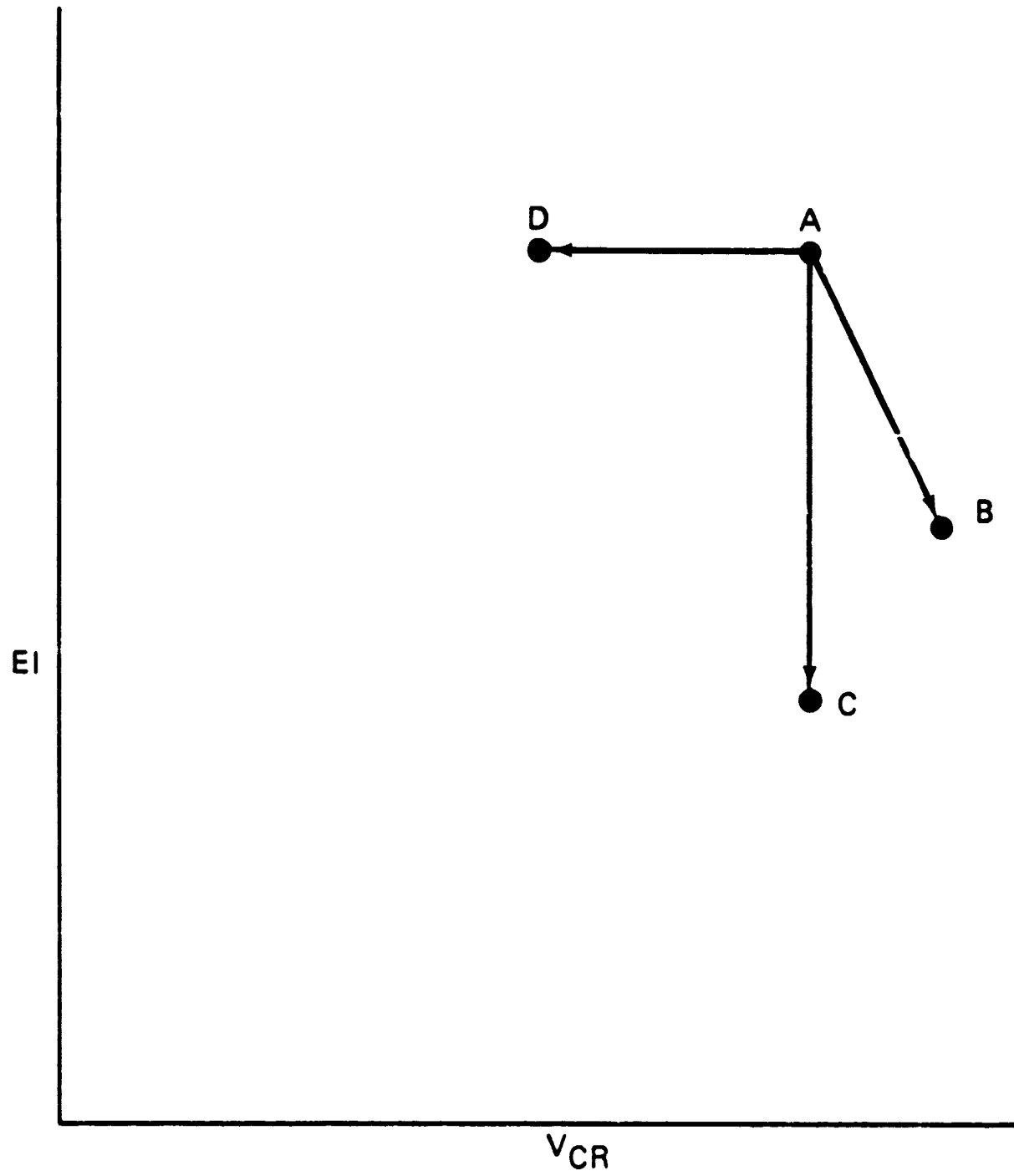


Figure 1. Typical EI vector diagram format

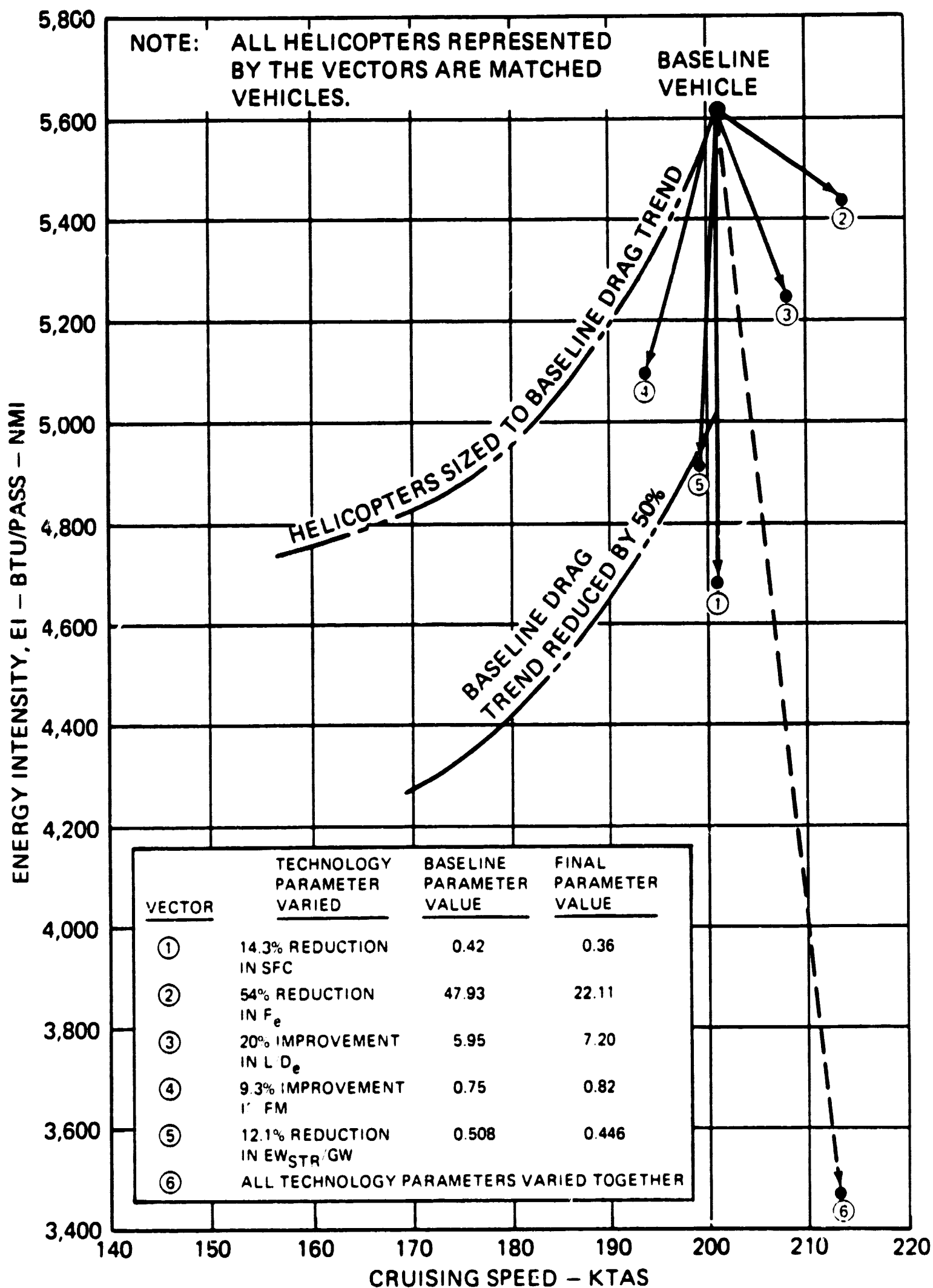


Figure 2. Effect of technological advances on the energy intensity of matched helicopters

results in an increase in cruising speed somewhat at the expense of EI. It is because of this matching that a large reduction in parasite drag (54 percent) does not reduce the EI in the amount that would be expected if no rotor limits were imposed. The EI reductions possible if these rotor limits are relaxed is discussed in Section 3.2.2.

Vector ③ represents a 20-percent increase in rotor  $L/D_e$ . As in the case of vector ②, reduced power required enables the helicopter to fly faster and thus dictates a solidity increase to achieve a matched vehicle.

Vector ④ represents a 9.3-percent improvement in figure of merit. The increased FM results in lower hover power requirements and thus lower installed power. This, in turn, results in an NRP cruising speed lower than the rotor-limit speed with the subsequent requirement to reduce the solidity to achieve a matched vehicle. Additionally, the reduced engine size results in lower fuel-consumption rates, and thus lowered EI.

Vector ⑤ represents a 12.1-percent reduction in structural empty/gross-weight fraction. The considerable reduction in gross weight caused by the reduced empty weight results in a decreased hover power requirement and lower installed power. As in the case of vector ④, this results in lower fuel-consumption rates, and, therefore, a reduced EI.

Vector ⑥ represents a combination of all technological improvements considered. Note that the solidity requirement for the combination is dictated by the need for a rotor-limit/cruising speed match for vector ②.

Figure 3 presents the effect of the same technological improvements on direct operating cost. Superimposed on the vectors is the locus of points for a series of helicopters sized to operate at cruising speeds less than NRP speed. Note that the baseline vehicle is located at the minimum DOC speed and that operation at lower speeds results in an increase in DOC. Since minimum DOC is obtained when the helicopter is operated at NRP speed and each vector represents a vehicle sized to operate at  $V_{NRP}$ , it is logical to assume that each vector in itself represents a minimum-DOC-point vehicle.

Table 2 lists the dimensional, weight, power, drag, speed, energy, and cost characteristics of the vehicles defined by the technological improvement vectors plotted in Figures 2 and 3.

Figure 4 illustrates the helicopter sizing trends overlaid on Figures 2 and 3. The upper trend line is the locus of points of a series of helicopters sized to the baseline helicopter ground rules. All vehicles represented by this line have a main-rotor solidity of 0.100. Only the baseline vehicle uses this solidity fully, flying its mission at its NRP/rotor-limit cruising speed. All the other helicopters on this line fly at less than their NRP cruising speed. The lower trend line is the locus of points of a series of helicopters sized to baseline helicopter ground rules – but with a 50-percent parasite-drag reduction. Up to a cruising speed of 200.8 knots (the baseline vehicle rotor-limit/NRP speed), the rotor solidity is equal to 0.100. In the area between points A and B, progressive increases in rotor-limit speed are achieved by increasing rotor solidity until a match between rotor-limit and NRP cruising speeds is achieved at point B.

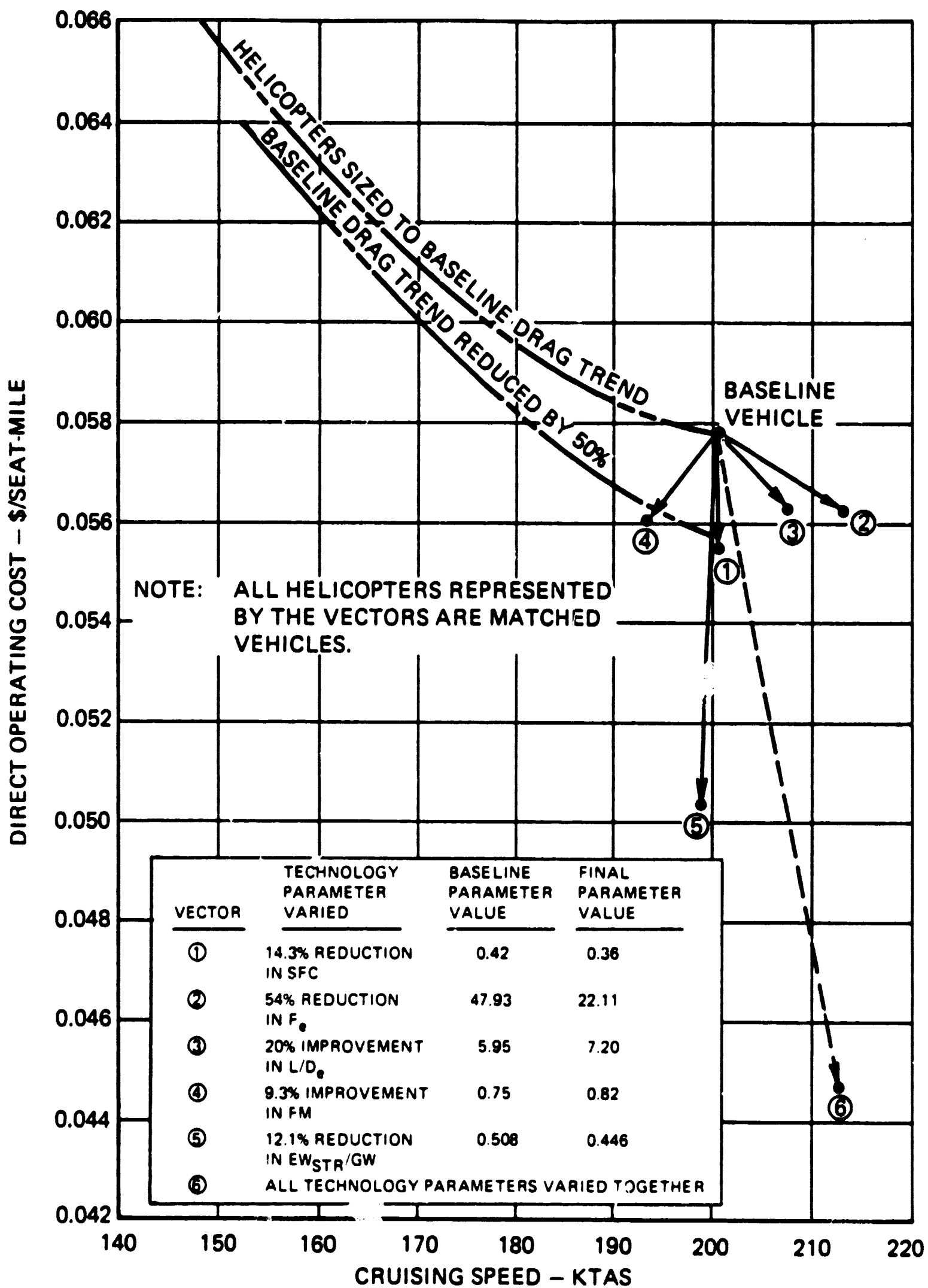


Figure 3. Effect of technological advances on the direct operating cost of matched helicopters.

**TABLE 2. TECHNOLOGY IMPROVEMENT VECTORS SUMMARY**

| Technology Configuration  | Vehicle Dimensional and Weight Characteristics |                   |                                |                     |                         |                | Vehicle Power and Drag Characteristics |                             |                                       | Vehicle Speed, Energy, and Cost Characteristics |                                       |   |                                    |
|---|--|-------------------|--------------------------------|---------------------|-------------------------|----------------|--|-----------------------------|---------------------------------------|---|---------------------------------------|---|------------------------------------|
|   | Gross Weight (lb)                              | Empty Weight (lb) | Mission Fuel <sup>①</sup> (lb) | Rotor Diameter (ft) | Rotor Cap/Stagger Ratio | Rotor Solidity | Rotor Figure of Merit <sup>②</sup>     | Total Installed Power (shp) | Parasite-Drag Area (ft <sup>2</sup> ) | Cruising Speed <sup>③</sup> (ktas)              | Energy Intensity (EI) (Btu/pass-n mi) | Percent Change in Energy Intensity, $\Delta EI/EI_{BASE}$ | Direct Operating Cost (\$/seat-mi) |
| Baseline  | 84,133   | 56,073            | 6,100                          | 87.5                | 0.113                   | 0.100          | 0.750                                  | 15,710                      | 47.93                                 | 200.8   | 5,612                                 | 0   | 0.0578                             |
| Baseline With 4.76% SFC Reduction   | 83,237   | 55,635            | 5,754                          | 87.0                | 0.114                   | 0.100          | 0.750                                  | 15,545                      | 47.68                                 | 200.8   | 5,287                                 | 5.8   | 0.0569                             |
| Baseline With 14.3% SFC Reduction   | 81,488   | 54,780            | 5,080                          | 86.1                | 0.115                   | 0.100          | 0.750                                  | 15,223                      | 47.20                                 | 200.8   | 4,680                                 | 16.6  | 0.0555                             |
| Baseline With 54% F <sub>e</sub> Reduction  | 84,631   | 56,877            | 5,907                          | 87.7                | 0.113                   | 0.106          | 0.743                                  | 15,957                      | 22.11                                 | 213.2   | 5,438                                 | 3.1   | 0.05625                            |
| Baseline With 20% L/D <sub>e</sub> Improvement  | 83,354   | 55,864            | 5,703                          | 87.0                | 0.114                   | 0.101          | 0.748                                  | 15,581                      | 47.69                                 | 208   | 5,247                                 | - 6.5   | 0.0563                             |
| Baseline With 9.3% FM Improvement   | 80,651   | 53,326            | 5,503                          | 85.6                | 0.116                   | 0.0975         | 0.822                                  | 13,747                      | 46.96                                 | 193.4   | 5,096                                 | 9.2   | 0.0561                             |
| Baseline With 12.1% EW <sub>STR</sub> /GW Reduction   | 72,971   | 45,910            | 5,335                          | 81.5                | 0.122                   | 0.100          | 0.750                                  | 13,657                      | 44.75                                 | 198.9   | 4,911                                 | 12.5  | 0.0564                             |
| Advanced-Technology Helicopter - 4.76% SFC Reduction (All technology improvements combined) | 70,058   | 44,398            | 4,260                          | 79.8                | 0.124                   | 0.106          | 0.812                                  | 12,139                      | 20.18                                 | 213.2   | 3,909                                 | 30.35   | 0.0457                             |
| Advanced-Technology Helicopter 14.3% SFC Reduction (All technology improvements combined)   | 68,924   | 43,910            | 3,775                          | 79.2                | 0.125                   | 0.106          | 0.812                                  | 11,947                      | 20.03                                 | 213.0   | 3,473                                 | 38.1  | 0.0447                             |

NOTES: ① Actual fuel consumed during mission; does not include reserves.  
 ② Rotor figure of merit at SL, 90°F conditions  
 ③ Cruising speed - NRP cruising speed - rotor-limit speed

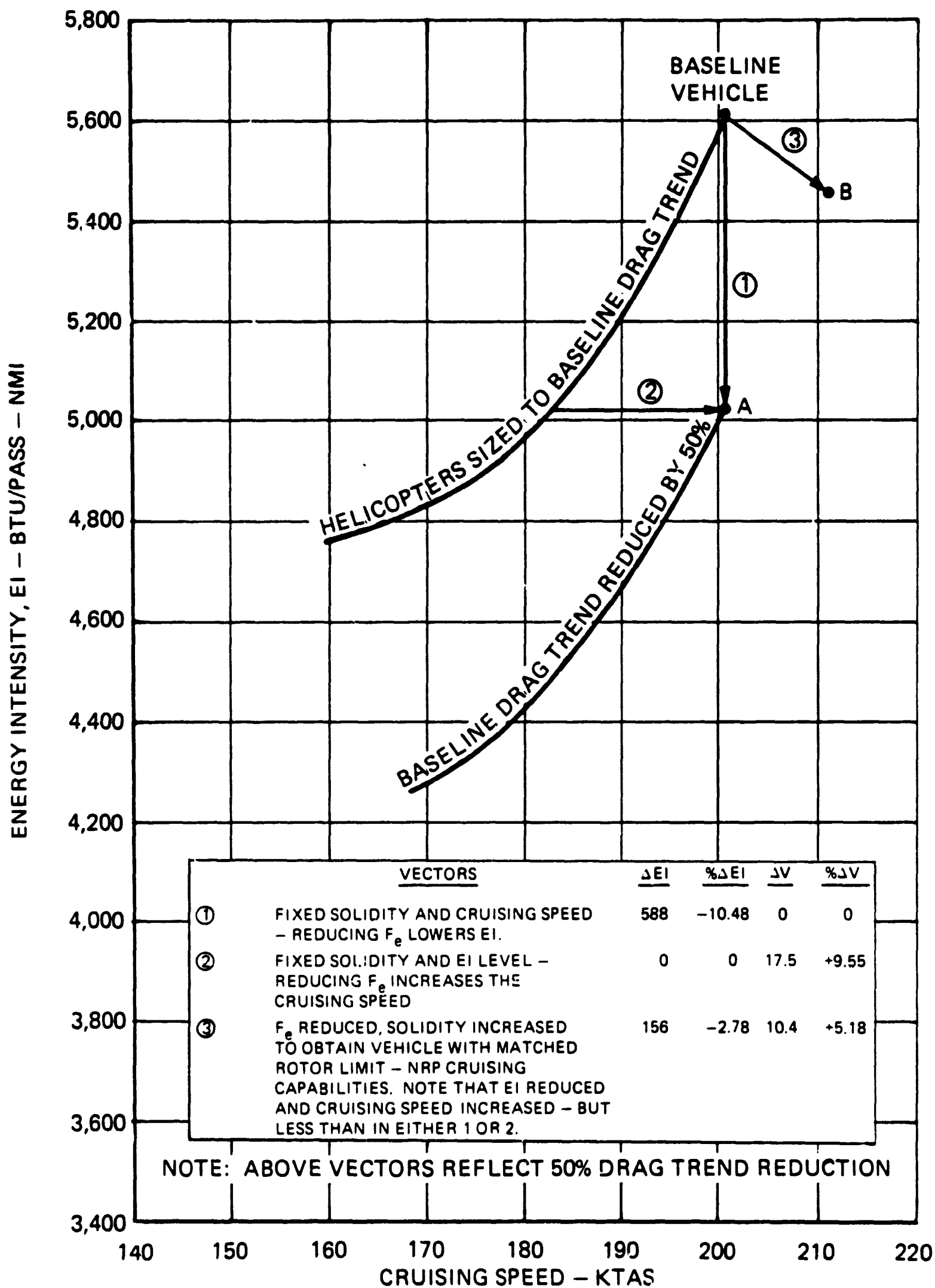


Figure 4. Effect of parasite-drag reduction and vehicle matching on energy intensity and cruising speed

Vectors ① , ② , and ③ depict three possible paths for employing parasite-drag reduction in the sizing of a helicopter.

Vector ① represents the result of applying a 50-percent parasite-drag reduction entirely to EI reduction. It is obtained simply by resizing the baseline helicopter with a 50-percent reduction in parasite drag and for operation at a fixed cruising speed of 200.8 knots.

Vector ② represents the result of applying a 50-percent parasite-drag reduction entirely to an increase in cruising speed. It is obtained by resizing a helicopter from the baseline drag trend line at a fixed level of EI and with a 50-percent reduction in parasite drag. Note that the resulting increased cruising speed corresponds to the baseline rotor-limit cruising speed of 200.8 knots.

Vector ③ illustrates the result of reducing parasite drag by 50-percent and then increasing rotor solidity to allow full utilization of the potential cruising-speed increase (i.e., matching the rotor-limit and NRP cruising speeds). This is the sizing path followed in NASA CR-144953. Note that the resulting vector exhibits smaller changes in both EI and cruising speed than vectors ① or ② , respectively.

**3.2.2 Effect of change in ground rules on energy intensity.** — Figure 5 illustrates the effect on vehicle EI and cruising speeds of relaxing the basic rotor-limit and cruising-speed sizing ground rules of CR-144953. Lines ① and ② are the upper and lower trend lines referred to in Figure 4. Line ③ is the locus of points of helicopters sized to the baseline helicopter ground rules — but with a 50-percent parasite-drag reduction, no rotor-limit speed restrictions, and with retreating-blade stall eliminated. Note that as the cruising speed decreases, lines ② and ③ begin to converge, illustrating a corresponding reduction in retreating-blade stall effects. Line ④ reflects, in addition to the assumptions of line ③ , a reduction in rotor solidity from 0.100 to 0.065. This reduced solidity results in maximum FM being achieved at the vehicle hover/takeoff conditions. The fact that this lower rotor solidity can be tolerated at the vehicle cruising speeds is a reflection of the removal of rotor-limit constraints.

It can be seen that line ④ represents the best EI reduction that might be achieved for the configuration and mission design ground rules. It should be emphasized, however, that this reduction depends on the following hypothesized assumptions:

1. Complete elimination of retreating-blade stall.
2. Either complete elimination of the rotor limits or the expansion of the limit boundaries sufficiently to allow the selection of rotor solidity based on maximizing hover performance only.

Vectors ① and ② refer to the two options available if parasite drag is reduced as presented in Figure 4. Vector ③ represents the application of a 50-percent  $F_e$  reduction and the elimination of retreating-blade stall and rotor limits to a baseline helicopter sized to cruise at NRP.



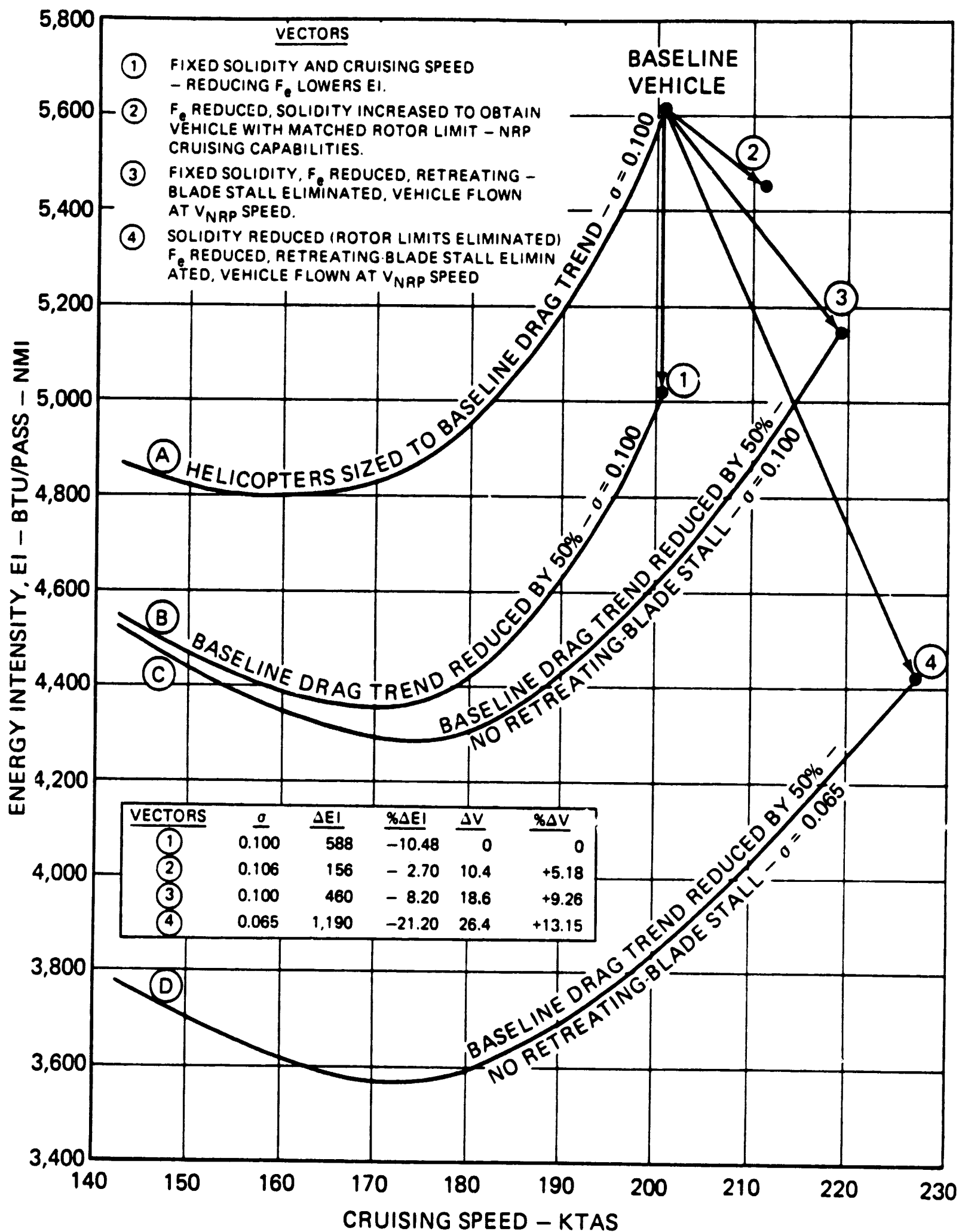


Figure 5. Effect of parasite-drag reduction, elimination of retreating-blade stall, and elimination of rotor limits on energy intensity and cruising speed

Vector ④ represents the vector ③ vehicle with rotor solidity reduced to maximize hover/takeoff performance.

Table 3 lists the dimensional, weight, power, drag, speed, and energy characteristics of the vehicles defined by the retreating-blade stall/rotor-limit vectors plotted in Figure 5.

Figure 6 is a vector representation of the effect on helicopter EI of hover-sizing and cruising-speed ground-rule change.

Vector ① illustrates the effect of resizing the baseline helicopter to a two-engine configuration without any attempt to meet the hover OEI requirement. The resulting helicopter exhibits substantial reductions in EI and DOC relative to the baseline. This is due to both the smaller size of the engines and their operation at more optimum partial-power settings (with resultant fuel savings), and additionally to the iterative nature of the sizing process. Note also that this vehicle is a minimum-DOC vehicle since its cruising speed is at NRP.

The substantial reduction in EI and DOC realized by this vector underscores the importance of further investigation into means for meeting the HOEI requirement with a two-engined configuration without recourse to engine oversizing.

Vector ② is the result of resizing the baseline helicopter to fly the design mission at 99 percent of best-range speed. Note that although the EI saving is over 13 percent, the DOC shows a marked increase. This is a result of resizing the helicopter at a cruising speed lower than VNRP. This trend of increasing DOC with decreasing cruising speed is well illustrated by the trend lines shown in Figure 3.

Vector ③ is included for reference purposes and shows the effect of reducing parasite drag by 50 percent and resizing the resulting helicopter to operate at the baseline rotor-limit speed of 200.8 knots.

Figure 7 presents the effects of ground-rule changes on direct operating cost.

Table 4 lists the dimensional, weight, power, drag, speed, energy, and cost characteristics of the vehicles defined by the ground-rule change vectors plotted in Figures 6 and 7.

**TABLE 3. RETREATING-BLADE STALL/ROTOR-LIMIT VECTORS SUMMARY**

| Vectors   | Vehicle Dimensional and Weight Characteristics |                   |                                |                     |                         |                | Vehicle Power and Drag Characteristics            |                                    |                             |                                       | Vehicle Speed and Energy Characteristics |                                       |   |
|---|--|-------------------|--------------------------------|---------------------|-------------------------|----------------|---|------------------------------------|-----------------------------|---------------------------------------|--|---------------------------------------|---|
|   | Gross Weight (lb)                              | Empty Weight (lb) | Mission Fuel <sup>①</sup> (lb) | Rotor Diameter (ft) | Rotor Gap/Stagger Ratio | Rotor Solidity | Rotor Operational Hover $C_T/\sigma$ <sup>②</sup> | Rotor Figure of Merit <sup>③</sup> | Total Installed Power (shp) | Parasite Drag Area (ft <sup>2</sup> ) | Cruising Speed (ktas)                    | Energy Intensity (EI) (Btu/pass-n mi) | Percent Change in Energy Intensity, $\Delta EI/EI_{BASE}$ |
| Baseline  | 84,133   | 56,073            | 6,100                          | 87.5                | 0.113                   | 0.100          | 0.070   | 0.75                               | 15,710                      | 47.93                                 | 200.8 <sup>④</sup>                       | 5,612                                 | 0   |
| 1. Baseline With 50% $F_e$ Reduction  | 82,576   | 55,312            | 5,461                          | 86.7                | 0.114                   | 0.100          | 0.070   | 0.75                               | 15,423                      | 23.75                                 | 200.8 <sup>⑤</sup>                       | 5,024                                 | 10.48   |
| 2. Baseline With 50% $F_e$ Reduction and Matched Rotor-Limit Cruising Capabilities            | 84,702   | 56,912            | 5,930                          | 87.8                | 0.113                   | 0.106          | 0.066   | 0.743                              | 15,970                      | 24.04                                 | 211.2 <sup>⑥</sup>                       | 5,456                                 | 2.7   |
| 3. Baseline With 50% $F_e$ Reduction, No Rotor Limits, No Retreating-Blade Stall <sup>⑨</sup> | 82,908   | 55,513            | 5,600                          | 86.8                | 0.114                   | 0.100          | 0.070   | 0.75                               | 15,495                      | 23.79                                 | 219.4 <sup>⑦</sup>                       | 5,152                                 | -8.2  |
| 4. Baseline With 50% $F_e$ Reduction, No Rotor Limits, No Retreating-Blade Stall <sup>⑨</sup> | 76,880   | 50,595            | 4,806                          | 83.6                | 0.119                   | 0.065          | 0.1076  | 0.787                              | 13,719                      | 22.95                                 | 227.2 <sup>⑧</sup>                       | 4,422                                 | -21.2   |

- NOTES:**
- ① Actual fuel consumed during mission, does not include reserves.
  - ② Hover  $C_T$  based on  $W/A = 7.0$  psf,  $V_T = 705$  fps,  $T/W = 1.1135$ , SL 90°F conditions.
  - ③ Rotor figure of merit at SL, 90°F conditions.
  - ④ Cruising speed = NRP cruising speed + rotor-limit speed.
  - ⑤ Cruising speed = rotor-limit speed.
  - ⑥ Cruising speed = NRP cruising speed + rotor-limit speed.
  - ⑦ Cruising speed = NRP cruising speed.
  - ⑧ Cruising speed = NRP cruising speed.
  - ⑨ It cannot be emphasized too strongly that vectors 3 and 4 are the result of the assumption that retreating-blade stall and rotor limits can somehow be eliminated. Vector 4 utilizes this latter assumption fully by reducing rotor solidity (to optimize hover efficiency) to a value well below that dictated by an NRP-rotor-limit cruising-speed match.

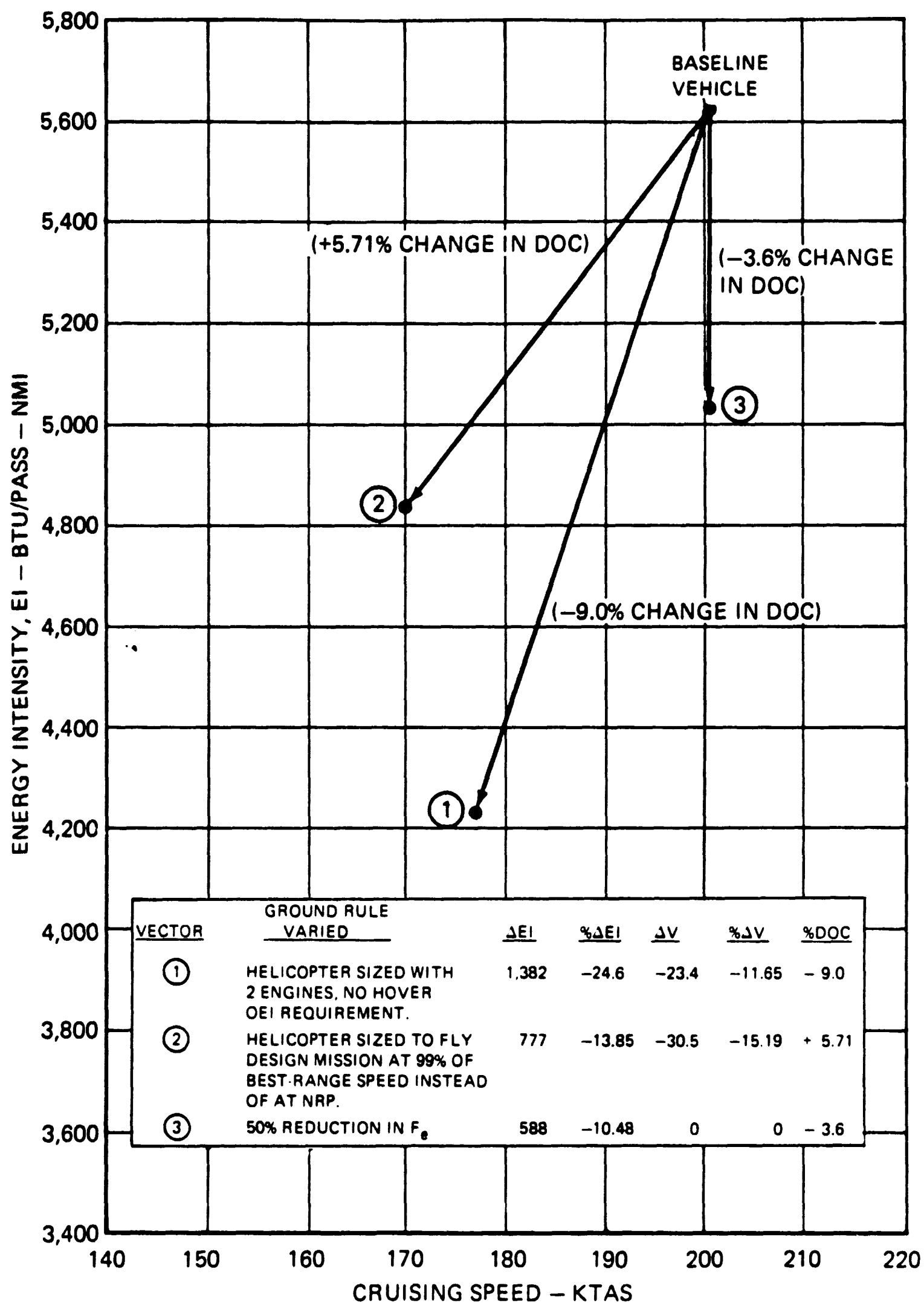


Figure 6. Effect of ground-rule changes on helicopter energy intensity

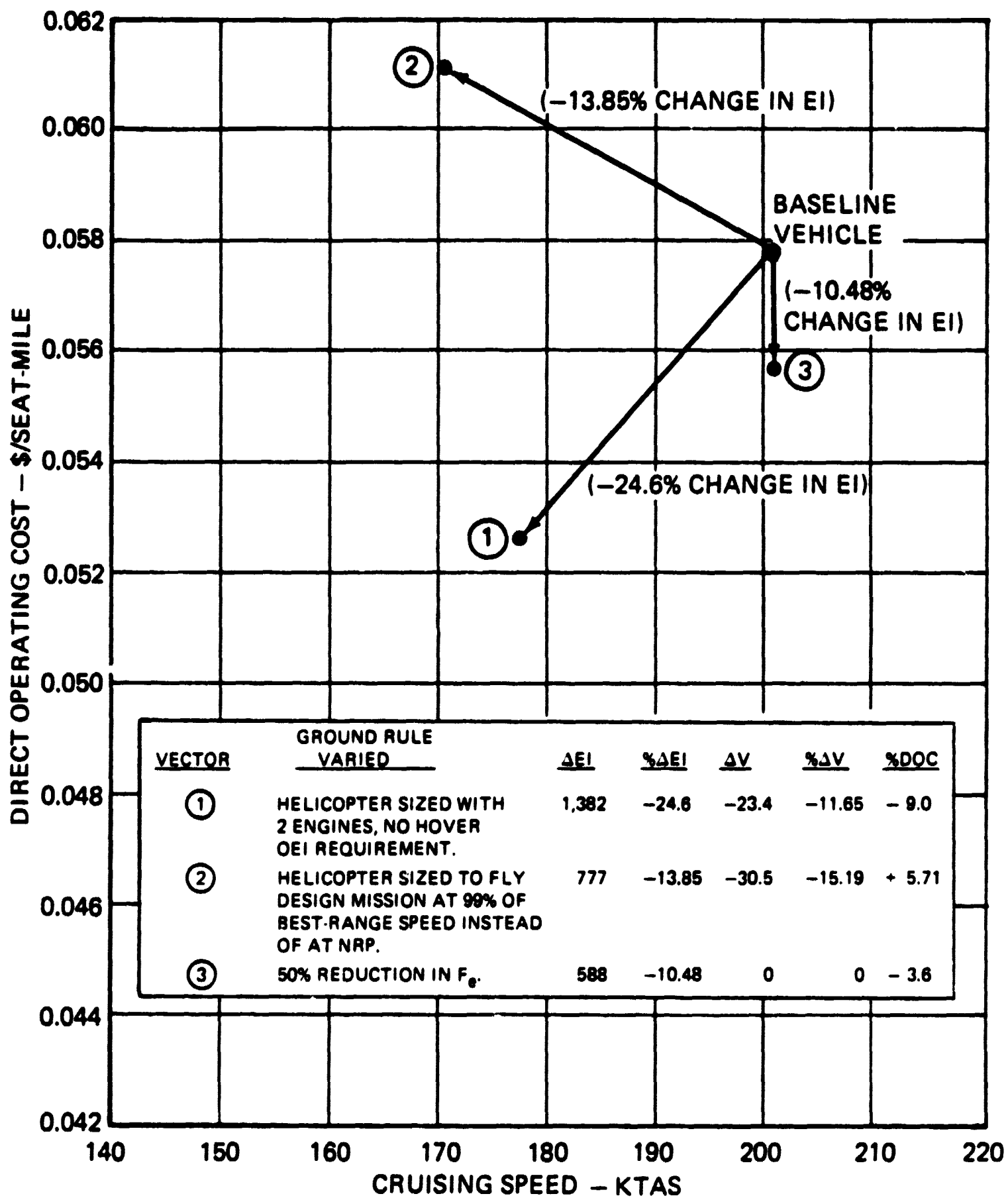


Figure 7. Effect of ground-rule changes on helicopter direct operating cost

**TABLE 4. GROUND-RULE CHANGE VECTORS SUMMARY**

| Ground Rules   | Vehicle Dimensional and Weight Characteristics |                   |                                |                     |                         |                | Vehicle Power and Drag Characteristics |                             |                                       | Vehicle Speed, Energy, and Cost Characteristics |                                       |   |                                    |
|--|--|-------------------|--------------------------------|---------------------|-------------------------|----------------|--|-----------------------------|---------------------------------------|---|---------------------------------------|---|------------------------------------|
|  | Gross Weight (lb)                              | Empty Weight (lb) | Mission Fuel <sup>①</sup> (lb) | Rotor Diameter (ft) | Rotor Gap/Stagger Ratio | Rotor Solidity | Rotor Figure of Merit <sup>②</sup>     | Total Installed Power (shp) | Parasite-Drag Area (ft <sup>2</sup> ) | Cruising Speed (ktas)                           | Energy Intensity (EI) (Btu/pass-n mi) | Percent Change in Energy Intensity, $\Delta EI/EI_{BASE}$ | Direct Operating Cost (\$/seat-mi) |
| Baseline   | 84,133   | 56,073            | 6,100                          | 87.5                | 0.113                   | 0.100          | 0.750                                  | 15,710                      | 47.93                                 | 200.8 <sup>③</sup>                              | 5,612                                 | 0   | 0.0578                             |
| Baseline -- 2 Engines -- No Hover OEI Rqmt                                   | 75,513   | 49,306            | 4,598                          | 82.9                | 0.120                   | 0.100          | 0.750                                  | 10,535                      | 45.50                                 | 177.4 <sup>④</sup>                              | 4,230                                 | -24.6   | 0.0526                             |
| Baseline -- Mission Flown at 99% V <sub>BR</sub> Instead of V <sub>NRP</sub> | 82,428   | 55,240            | 5,255                          | 86.6                | 0.115                   | 0.100          | 0.750                                  | 15,396                      | 47.46                                 | 170.3 <sup>⑤</sup>                              | 4,835                                 | -13.85  | 0.0611                             |
| Baseline 50% F <sub>e</sub> Reduction  | 82,576   | 55,312            | 5,461                          | 86.7                | 0.114                   | 0.100          | 0.750                                  | 15,423                      | 23.75                                 | 200.8 <sup>⑥</sup>                              | 5,024                                 | -10.48  | 0.0557                             |

**NOTES:**

- ① Actual fuel consumed during mission; does not include reserves.
- ② Rotor figure of merit at SL, 90°F conditions.
- ③ Cruising speed = NRP cruising speed = rotor-limit speed.
- ④ Cruising speed = NRP cruising speed.
- ⑤ Cruising speed = 99% best-range speed.
- ⑥ Cruising speed = rotor-limit speed.

## **4.0 CONCLUDING REMARKS**

The conclusions arrived at in this addendum can be summarized as follows:

1. Unmatched helicopters exhibit greater reductions in energy intensity than matched configurations. However, matched helicopters are always minimum-direct-operating-cost vehicles. Therefore, the choice between matched and unmatched helicopters must reflect a conscious decision between the goals of maximum-energy-intensity reduction and minimum-direct-operating-cost operation.
2. The manner in which a parasite-drag reduction is applied in the resizing of a helicopter is important in determining the level of EI reduction obtained. Thus, the relatively small EI reduction noted for the matched vehicle of CR-144953, which was resized with a 54-percent reduction in parasite drag, was due to that aircraft's utilization of its reduced parasite power in increasing design cruising speed rather than operating at a fixed cruising speed and reduced fuel (energy) consumption.
3. Substantial reductions in EI could be obtained if a satisfactory way could be found to increase rotor efficiency by simultaneously performing the contradictory tasks of reducing retreating-blade stall and reducing solidity requirements (through the expansion of rotor forward-flight operating limits).
4. Substantial reductions in both EI and DOC could be realized if a means could be found for meeting the HOEI requirement with a two-engine configuration without recourse to engine oversizing.